Outline

- Introduction & architectural issues
- Data distribution
 - ■Fragmentation
 - ■Data Allocation
- ☐ Distributed query processing
- ☐ Distributed query optimization
- ☐ Querying multidatabase systems
- ☐ Distributed transactions & concurrency control
- □ Distributed reliability
- □ Database replication
- ☐ Parallel database systems
- ☐ Database integration & querying
- ☐ Advanced topics

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Design Problem

■ In the general setting:

Making decisions about the placement of *data* and *programs* across the sites of a computer network as well as possibly designing the network itself.

- In Distributed DBMS, the placement of applications entails
 - placement of the distributed DBMS software; and
 - placement of the applications that run on the database

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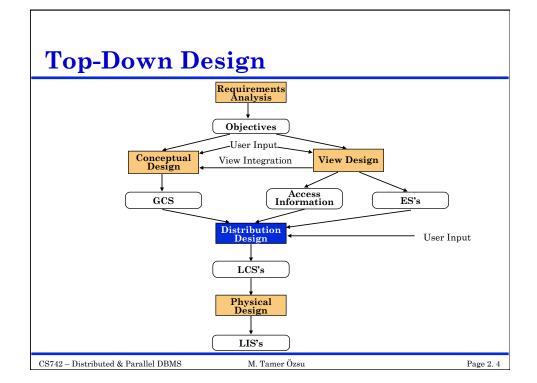
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Distribution Design

- Top-down
 - mostly in designing systems from scratch
 - mostly in homogeneous systems
- Bottom-up
 - when the databases already exist at a number of sites

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Distribution Design Issues

- Why fragment at all?
- 2 How to fragment?
- 8 How much to fragment?
- 4 How to test correctness?
- 6 How to allocate?
- 6 Information requirements?

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Fragmentation

- Can't we just distribute relations?
- What is a reasonable unit of distribution?
 - Relation
 - Views are subsets of relations → locality
 - ◆ Extra communication
 - Fragments of relations (sub-relations)
 - Concurrent execution of a number of transactions that access different portions of a relation
 - Views that cannot be defined on a single fragment will require extra processing
 - Semantic data control (especially integrity enforcement) more difficult

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Fragmentation Alternatives – Horizontal

 ${
m PROJ_1}$: projects with budgets less than \$200,000

 ${
m PROJ_2}$: projects with budgets greater than or equal to $\$200,\!000$

PROJ

PNO	PNAME	BUDGET	LOC
P1	Instrumentation Database Develop. CAD/CAM Maintenance CAD/CAM	150000	Montreal
P2		135000	New York
P3		250000	New York
P4		310000	Paris
P5		500000	Boston

PROJ₁

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal
P2	Database Develop.	135000	New York

PROJ₂

PNO	PNAME	BUDGET	LOC
P3	CAD/CAM	250000	New York
P4	Maintenance	310000	Paris
P5	CAD/CAM	500000	Boston

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Fragmentation Alternatives – Vertical

 $PROJ_1$: information about project budgets

PROJ₂: information about project names and locations

PROJ

PNO	PNAME	BUDGET	LOC
P1	Instrumentation Database Develop. CAD/CAM Maintenance CAD/CAM	150000	Montreal
P2		135000	New York
P3		250000	New York
P4		310000	Paris
P5		500000	Boston

PROJ₁

PNO	BUDGET
P1	150000
P2	135000
P3	250000
P4	310000
P5	500000

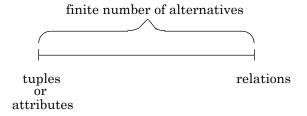
PROJ₂

PNO	PNAME	LOC
P1 P2 P3 P4	Instrumentation Database Develop. CAD/CAM Maintenance	New York Paris
P5	CAD/CAM	Boston

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Degree of Fragmentation



Finding the suitable level of partitioning within this range

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Correctness of Fragmentation

- Completeness
 - Decomposition of relation R into fragments $R_1, R_2, ..., R_n$ is complete if and only if each data item in R can also be found in some R_i
- Reconstruction
 - ullet If relation R is decomposed into fragments $R_1,\,R_2,\,...,\,R_n$, then there should exist some relational operator ∇ such that

$$R = \nabla_{1 \le i \le n} R_i$$

- Disjointness
 - If relation R is decomposed into fragments $R_1, R_2, ..., R_n$, and data item d_i is in R_j , then d_i should not be in any other fragment R_k $(k \neq j)$.

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Allocation Alternatives

- Non-replicated
 - partitioned: each fragment resides at only one site
- Replicated
 - fully replicated : each fragment at each site
 - partially replicated : each fragment at some of the sites
- Rule of thumb:

 $\label{eq:constraints} \begin{tabular}{ll} \hline If & \frac{read-only\ queries}{update\ quries} \ge 1\ replication\ is\ advantageous, \\ otherwise\ replication\ may\ cause\ problems \\ \hline \end{tabular}$

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Information Requirements

- Four categories:
 - Database information
 - Application information
 - Communication network information
 - Computer system information

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Fragmentation

- Horizontal Fragmentation (HF)
 - Primary Horizontal Fragmentation (PHF)
 - Derived Horizontal Fragmentation (DHF)
- Vertical Fragmentation (VF)
- Hybrid Fragmentation (HF)

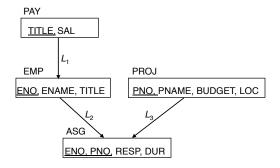
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PHF - Information Requirements

- Database information
 - Relationship



Cardinality of each relation: card(R)

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PHF - Information Requirements

- Application Information
 - simple predicates : Given $R[A_1, A_2, ..., A_n]$, a simple predicate p_j is

$$p_i: A_i \ \theta \ Value$$

where $\theta \in \{=,<,\leq,>,\geq,\neq\}$, $Value \in D_i$ and D_i is the domain of A_i .

For relation R we define $Pr = \{p_1, p_2, ..., p_m\}$

Example:

PNAME = "Maintenance"

 $BUDGET \leq 200000$

• minterm predicates : Given R and $Pr = \{p_1, p_2, ..., p_m\}$ define $M = \{m_1, m_2, ..., m_r\}$ as

$$M = \{\; m_i \,|\; m_i = \; \textstyle \bigwedge_{p_j \in Pr} \; p_j^{\; *} \;\}, \; 1 \leq j \leq m, \; 1 \leq i \leq z$$
 where $p_i^{\; *} = p_i$ or $p_i^{\; *} = \neg (p_i).$

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PHF - Minterm Examples

■ Simple predicates on PROJ (partial)

 p_1 : LOC = "Montreal"

p₂: LOC="New York"

 p_3 : LOC = "Paris"

 p_4 : BUDGET ≤ 200000

 p_5 : BUDGET ≤ 200000

■ Minterm predicates on PROJECT (Partial)

 m_1 : LOC = "Montreal" \land BUDGET ≤ 200000

 m_2 : **NOT**(LOC="Montreal") \land BUDGET ≤ 200000

 m_3 : LOC = "Montreal" \land **NOT**(BUDGET \le 200000)

 m_4 : **NOT**(LOC = "Montreal") \land **NOT**(BUDGET ≤ 200000)

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PHF - Information Requirements

- Application information.
 - minterm selectivities: $sel(m_i)$.
 - ◆ The number of tuples of the relation that would be accessed by a user query which is specified according to a given minterm predicate m_i.
 - access frequencies: $acc(q_i)$.
 - ◆ The frequency with which a user application *qi* accesses data.
 - ◆ Access frequency for a minterm predicate can also be defined.

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Primary Horizontal Fragmentation

Definition:

$$R_j = \sigma_{F_i}(r), \quad 1 \le j \le w$$

where F_j is a selection formula, which is (preferably) a minterm predicate.

Therefore,

A horizontal fragment R_i of relation R consists of all the tuples of R which satisfy a minterm predicate m_i .



Given a set of minterm predicates M, there are as many horizontal fragments of relation R as there are minterm predicates.

Set of horizontal fragments also referred to as *minterm fragments*.

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PHF - Algorithm

Given: A relation R, the set of simple predicates Pr Output: The set of fragments of R, $F_R = \{R_1, R_2, \dots, R_w\}$ that obey the fragmentation rules.

Preliminaries:

- ullet Pr should be complete
- ullet Pr should be minimal

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Completeness of Simple Predicates

- A set of simple predicates Pr is said to be *complete* if and only if the accesses to the tuples of the minterm fragments defined on Pr requires that two tuples of the same minterm fragment have the same probability of being accessed by any application.
- Example :
 - Assume PROJ(PNO,PNAME,BUDGET,LOC) has two applications defined on it.
 - Find the budgets of projects at each location. (1)
 - Find projects with budgets less than or equal to \$200000. (2)

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Completeness of Simple Predicates

According to (1), $Pr = \{ \text{LOC} = \text{``Montreal''}, \text{LOC} = \text{``New York''}, \text{LOC} = \text{``Paris''} \}$ which is not complete with respect to (2). $Modify \\ Pr = \{ \text{LOC} = \text{``Montreal''}, \text{LOC} = \text{``New York''}, \text{LOC} = \text{``Paris''}, \\ \text{BUDGET} \leq 200000, \text{BUDGET} > 200000 \}$ which is complete.

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Minimality of Simple Predicates

- If a predicate influences how fragmentation is performed, (i.e., causes a fragment f to be further fragmented into, say, f_i and f_j) then there should be at least one application that accesses f_i and f_j differently.
- In other words, the simple predicate should be *relevant* in determining a fragmentation.
- If all the predicates of a set Pr are relevant, then Pr is minimal.

$$\frac{acc(m_i)}{card(f_i)} \neq \frac{acc(m_j)}{card(f_i)}$$

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Minimality of Simple Predicates

Example:

$$\label{eq:pr} \begin{split} Pr = & \{ \text{LOC="Montreal",LOC="New York", LOC="Paris",} \\ & \text{BUDGET\leq200000,BUDGET$>$200000} \} \end{split}$$

is minimal (in addition to being complete). However, if we add

PNAME = "Instrumentation"

a fragment could be accessed by many for the same query

then Pr is not minimal.

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COM_MIN Algorithm

Given: a relation *R* and a set of simple

predicates Pr

Output: a *complete* and *minimal* set of simple

predicates Pr' for Pr

Rule 1: a relation or fragment is partitioned into at least two parts which are accessed differently by at least one application.

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COM_MIN Algorithm

- Initialization :
 - find a $p_i \in Pr$ such that p_i partitions R according to $Rule\ 1$
 - set $Pr' = p_i$; $Pr \leftarrow Pr p_i$; $F \leftarrow f_i$
- ${f 2}$ Iteratively add predicates to Pr' until it is complete
 - find a $p_j \in Pr$ such that p_j partitions some f_k defined according to minterm predicate over Pr' according to $Rule\ 1$
 - set $Pr' = Pr' \cup p_i$; $Pr \leftarrow Pr p_i$; $F \leftarrow F \cup f_i$
 - if $\exists p_k \in Pr'$ which is nonrelevant then

$$Pr' \leftarrow Pr' - p_k$$

 $F \leftarrow F - f_k$

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PHORIZONTAL Algorithm

Makes use of COM_MIN to perform fragmentation.

Input: a relation R and a set of simple predicates Pr

Output: a set of minterm predicates *M* according to which relation *R* is to be fragmented

- $Pr' \leftarrow \text{COM_MIN}(R,Pr)$
- **8** determine the set *I* of implications among $p_i \in Pr$
- eliminate the contradictory minterms from *M*

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PHF - Example

- Two candidate relations : PAY and PROJ.
- Fragmentation of relation PROJ
 - Applications:
 - ◆ Find the name and budget of projects given their location
 - · Issued at three sites
 - ◆ Access project information according to budget
 - one site accesses <200000 other accesses ≥200000
 - Simple predicates
 - For application (1)
 - p_1 : LOC = "Montreal"
 - p_2 : LOC = "New York"
 - p_3 : LOC = "Paris"
 - For application (2)
 - $p_4: \mathrm{BUDGET} \leq 200000$
 - p_5 : BUDGET > 200000
 - $Pr = Pr' = \{p_1, p_2, p_3, p_4, p_5\}$

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PHF - Example

- Fragmentation of relation PROJ continued
 - Minterm fragments left after elimination

```
m_1: (LOC = "Montreal") \land (BUDGET \leq 200000)
```

 m_2 : (LOC = "Montreal") \land (BUDGET >200000)

 m_3 : (LOC = "New York") \land (BUDGET \leq 200000)

 m_4 : (LOC = "New York") \land (BUDGET \geq 200000)

 m_5 : (LOC = "Paris") \land (BUDGET \leq 200000)

 m_6 : (LOC = "Paris") \land (BUDGET \ge 200000)

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PHF - Example

PROJ₁

PROJ₂

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal

PNO	PNAME	BUDGET	LOC
P2	Database Develop.	135000	New York

PROJ₄

$PROJ_6$

PNO	PNAME	BUDGET	LOC
P3	CAD/CAM	250000	New York

PNO	PNAME	BUDGET	LOC
P4	Maintenance	310000	Paris

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PHF - Correctness

- Completeness
 - \bullet Since Pr' is complete and minimal, the selection predicates are complete
- Reconstruction
 - If relation R is fragmented into $F_R = \{R_1, R_2, ..., R_r\}$

$$R = \bigcup_{\forall R_i \in FR} R_i$$

- Disjointness
 - Minterm predicates that form the basis of fragmentation should be mutually exclusive.

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Vertical Fragmentation

- Has been studied within the centralized context
 - design methodology
 - physical clustering
- More difficult than horizontal, because more alternatives exist.

Two approaches:

- grouping
 - ♦ attributes to fragments
- splitting
 - relation to fragments

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Vertical Fragmentation

- Overlapping fragments
 - grouping
- Non-overlapping fragments
 - splitting

We do not consider the replicated key attributes to be overlapping.

Advantage:

Easier to enforce functional dependencies (for integrity checking etc.)

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VF - Information Requirements

- Application Information
 - Attribute affinities
 - a measure that indicates how closely related the attributes are
 - ◆ This is obtained from more primitive usage data
 - Attribute usage values
 - Given a set of queries $Q = \{q_1, q_2, ..., q_q\}$ that will run on the $R[A_1, A_2, ..., A_n],$

$$use(q_{i'}A_j) = \begin{cases} 1 \text{ if attribute } A_j \text{ is referenced by query } q_i \\ 0 \text{ otherwise} \end{cases}$$

 $use(q_i, \bullet)$ can be defined accordingly

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VF – Definition of $use(q_i,A_j)$

Consider the following 4 queries for relation PROJ

 q_1 :SELECT BUDGET q_2 : **SELECT** PNAME, BUDGET **PROJ**

FROM PROJ

WHERE PNO=Value

 q_4 : **SELECT SUM**(BUDGET)

 q_3 :SELECT PNAME FROM PROJ

WHERE LOC=Value

FROM **PROJ** WHERE LOC=Value

FROM

Let A_1 = PNO, A_2 = PNAME, A_3 = BUDGET, A_4 = LOC

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VF – Affinity Measure $aff(A_i,A_i)$

The attribute affinity measure between two attributes A_i and A_j of a relation $R[A_1, A_2, ..., A_n]$ with respect to the set of applications $Q = (q_1, q_2, ..., q_q)$ is defined as follows:

$$aff(A_i, A_j) = \sum_{\text{all queries that access } A_i \text{ and } A_j$$

query access =
$$\sum_{\text{all sites}}$$
 access frequency of a query * $\frac{\text{access}}{\text{execution}}$

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VF – Calculation of $aff(A_i, A_i)$

Assume each query in the previous example accesses the attributes once during each execution.

Also assume the access frequencies =

Then

Then
$$aff(A_1, A_3) = 15*1 + 20*1 + 10*1 = 45$$
 and the attribute affinity matrix AA is $A_1 = \begin{bmatrix} A_1 & A_2 & A_3 & A_4 \\ 45 & 0 & 45 & 0 \\ 0 & 80 & 5 & 75 \\ 45 & 5 & 53 & 3 \\ A_4 & 0 & 75 & 3 & 78 \end{bmatrix}$

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VF - Clustering Algorithm

- Take the attribute affinity matrix *AA* and reorganize the attribute orders to form clusters where the attributes in each cluster demonstrate high affinity to one another.
- Bond Energy Algorithm (BEA) has been used for clustering of entities. BEA finds an ordering of entities (in our case attributes) such that the global affinity measure is maximized.

$$AM = \sum_{i} \sum_{j}$$
 (affinity of A_i and A_j with their neighbors)

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Bond Energy Algorithm

Input: The AA matrix

Output: The clustered affinity matrix *CA* which is a perturbation of *AA*

- *Initialization*: Place and fix one of the columns of *AA* in *CA*.
- ② Iteration: Place the remaining n-i columns in the remaining i+1 positions in the CA matrix. For each column, choose the placement that makes the most contribution to the global affinity measure.
- Row order: Order the rows according to the column ordering.

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Bond Energy Algorithm

"Best" placement? Define contribution of a placement:

$$cont(A_i, A_k, A_l) = 2bond(A_i, A_k) + 2bond(A_k, A_l) - 2bond(A_i, A_l)$$

where
$$bond(A_{x\prime}A_y) = \sum_{x=1}^n aff(A_{z\prime}A_x)aff(A_{z\prime}A_y)$$

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BEA - Example

Consider the following AA matrix and the corresponding CA matrix where A_1 and A_2 have been placed. Place A_3 :

Ordering (0-3-1):

 $\begin{array}{ll} cont(A_0,\!A_3,\!A_1) & = 2bond(A_0\;,A_3) + 2bond(A_3\;,A_1) - 2bond(A_0\;,A_1) \\ & = 2*\;0 + 2*\;4410 - 2*0 = 8820 \end{array}$

Ordering (1-3-2):

 $cont(A_1, A_3, A_2) = 2bond(A_1, A_3) + 2bond(A_3, A_2) - 2bond(A_1, A_2)$

= 2*4410 + 2*890 - 2*225 = 10150

Ordering (2-3-4):

 $cont (A_2, A_3, A_4) = 1780$

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BEA - Example

■ Therefore, the CA matrix has the form A_1 A_3 A_2

■ When A_4 is placed, the final form of the CA matrix (after row organization) is $A_1 \ A_3 \ A_2 \ A_4$

$$A_1$$
 $\begin{bmatrix} 45 & 45 & 0 & 0 \\ A_3 & 45 & 53 & 5 & 3 \\ A_2 & 0 & 5 & 80 & 75 \\ A_4 & 0 & 3 & 75 & 78 \end{bmatrix}$

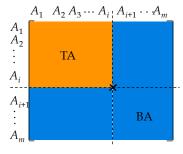
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VF - Algorithm

How can you divide a set of clustered attributes $\{A_1, A_2, ..., A_n\}$ into two (or more) sets $\{A_1, A_2, ..., A_i\}$ and $\{A_i, ..., A_n\}$ such that there are no (or minimal) applications that access both (or more than one) of the sets.



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VF - ALgorithm

Define

TQ = set of applications that access only TA

BQ = set of applications that access only BA

OQ = set of applications that access both TA and BA

and

CTQ =total number of accesses to attributes by applications that access only TA

CBQ =total number of accesses to attributes by applications that access only BA

COQ =total number of accesses to attributes by applications that access both TA and BA

Then find the point along the diagonal that maximizes

 $CTQ*CBQ-COQ^2$

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VF - Algorithm

Two problems:

- Cluster forming in the middle of the *CA* matrix
 - Shift a row up and a column left and apply the algorithm to find the "best" partitioning point
 - Do this for all possible shifts
 - Cost $O(m^2)$
- 2 More than two clusters
 - *m*-way partitioning
 - try 1, 2, ..., *m*–1 split points along diagonal and try to find the best point for each of these
 - Cost $O(2^m)$

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VF - Correctness

A relation R, defined over attribute set A and key K, generates the vertical partitioning $F_R = \{R_1, R_2, ..., R_r\}$.

- Completeness
 - The following should be true for *A*:

$$A = \bigcup A_{R_i}$$

- Reconstruction
 - Reconstruction can be achieved by

$$R = \bowtie K_i, \forall R_i \in F_R$$

- Disjointness
 - TID's are not considered to be overlapping since they are maintained by the system
 - Duplicated keys are not considered to be overlapping

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Fragment Allocation

■ Problem Statement

Given

$$\begin{split} F &= \{F_1,\,F_2,\,\ldots,\,F_n\} &\quad \text{fragments} \\ S &= \!\! \{S_1,\,S_2,\,\ldots,\,S_m\} &\quad \text{network sites} \\ Q &= \{q_1,\,q_2,\ldots,\,q_q\} &\quad \text{applications} \end{split}$$

Find the "optimal" distribution of *F* to *S*.

- Optimality
 - Minimal cost
 - ◆ Communication + storage + processing (read & update)
 - ◆ Cost in terms of time (usually)
 - Performance

Response time and/or throughput

- Constraints
 - ◆ Per site constraints (storage & processing)

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Information Requirements

- Database information
 - selectivity of fragments
 - size of a fragment
- Application information
 - access types and numbers
 - access localities
- Communication network information
 - unit cost of storing data at a site
 - unit cost of processing at a site
- Computer system information
 - bandwidth
 - latency
 - communication overhead

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Allocation Model

General Form

min(Total Cost)

subject to

response time constraint

 $storage\ constraint$

processing constraint

Decision Variable

 $X_{ij} = \begin{cases} 1 \text{ if fragment } F_i \text{ is stored at site } S_j \\ 0 \text{ otherwise} \end{cases}$

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Allocation Model

■ Total Cost

$$\sum_{\rm all~queries} {\rm query~processing~cost~+}$$

$$\sum_{\rm all~sites} \sum_{\rm all~fragments} {\rm cost~of~storing~a~fragment~at~a~site}$$

■ Storage Cost (of fragment F_j at S_k)

(unit storage cost at S_k) * (size of F_j) * x_{jk}

■ Query Processing Cost (for one query)

processing component + transmission component

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